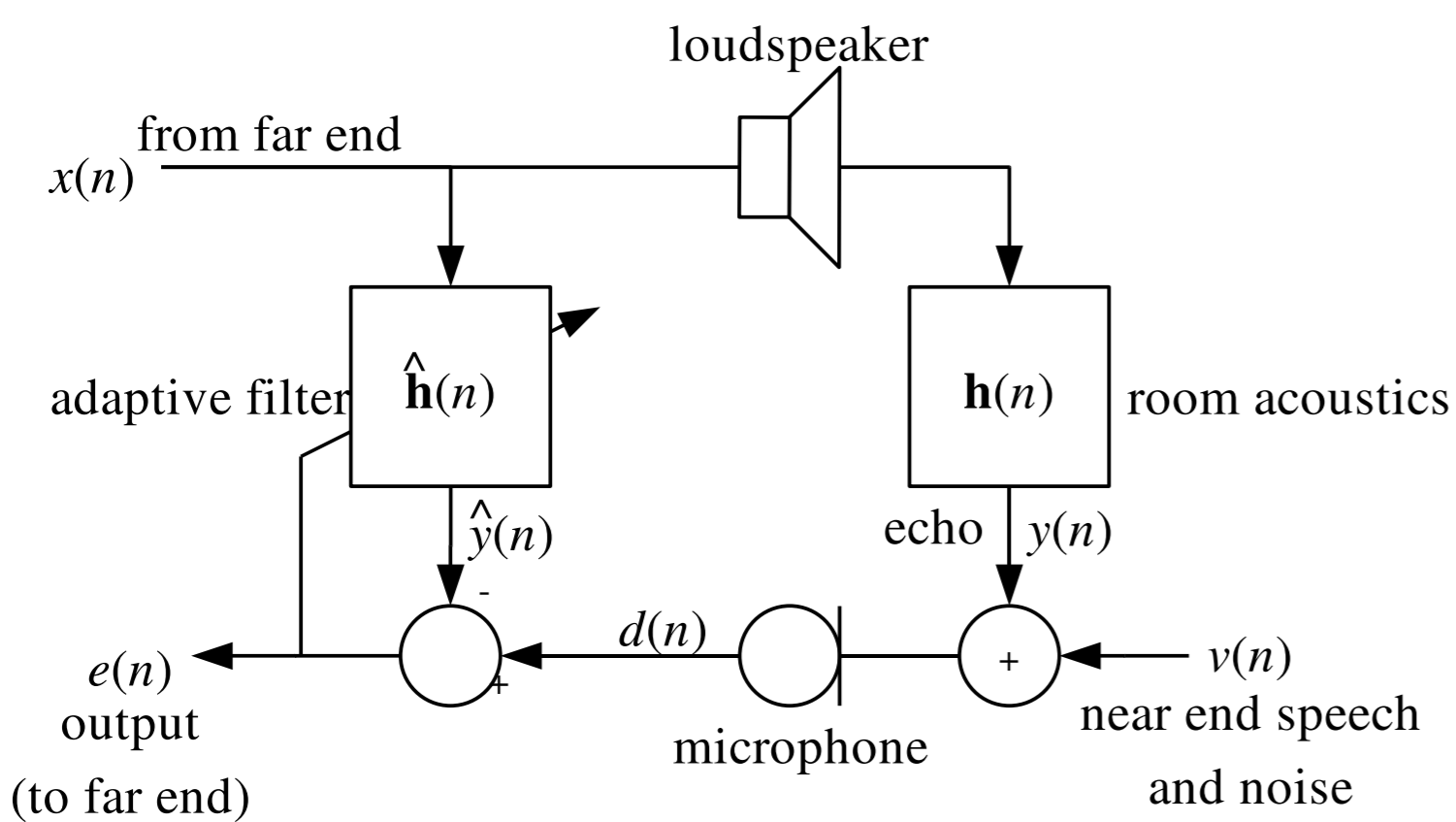


## A NEW ROBUST FREQUENCY-DOMAIN ECHO CANCELLER WITH CLOSED-LOOP LEARNING RATE ADAPTATION

**Context:** Acoustic echo cancellation in the presence of double-talk and noise

**Problem:** How to select the optimal learning rate

**Solution:** Gradient-adaptive learning rate adaptation



**Optimal Learning Rate:**

$$\mu_{opt}(n) = \frac{E[r^2(n)]}{E[e^2(n)]}$$

- Depends on the Echo Return Loss Enhancement (ERLE)
- ERLE not directly measurable
- Optimal rate never zero when far end is active

### Multidelay Block Frequency Domain (MDF) Adaptive Filter

- $K$  blocks of  $N$  samples (FFT on  $2N$  samples)

MDF algorithm summary

$$\begin{aligned} \underline{e}(\ell) &= \underline{d}(\ell) - \underline{y}(\ell) \\ \underline{y}(\ell) &= \mathbf{G}_1 \underline{\mathbf{X}}(\ell) \hat{\underline{\mathbf{h}}}(\ell) \\ \hat{\underline{\mathbf{h}}}(\ell+1) &= \hat{\underline{\mathbf{h}}}(\ell) + \mathbf{G}_2 \underline{\mu}(\ell) \nabla \hat{\underline{\mathbf{h}}}(\ell) \\ \nabla \hat{\underline{\mathbf{h}}}(\ell) &= \Phi_{\mathbf{xx}}^{-1}(\ell) \underline{\mathbf{X}}^H(\ell) \underline{e}(\ell) \end{aligned}$$

### Proposed Solution

- Frequency-dependent learning rate
- Online optimisation of the learning rate
- Based on the behaviour of the stochastic gradient

$$\mu_k(\ell) = \min \left( \eta(\ell) \frac{|\hat{\underline{y}}_k(\ell)|^2}{|\underline{e}_k(\ell)|^2}, \mu_0 \right)$$

Hard to estimate

Easy to estimate

Main Parameter

$$\eta(\ell+1) = \eta(\ell) \exp \left[ \rho \frac{|\hat{\underline{y}}_k(\ell)|^2 \Re \{ \underline{\psi}^H(\ell) \nabla \hat{\underline{\mathbf{h}}}(\ell) \}}{|\underline{e}_k(\ell)|^2 \sum_k \Re \{ \psi_k^*(\ell) \nabla \hat{h}_k(\ell) \}} \right]$$

$$\underline{\psi}(\ell+1) = \alpha \underline{\psi}(\ell) + \nabla \hat{\underline{\mathbf{h}}}(\ell)$$

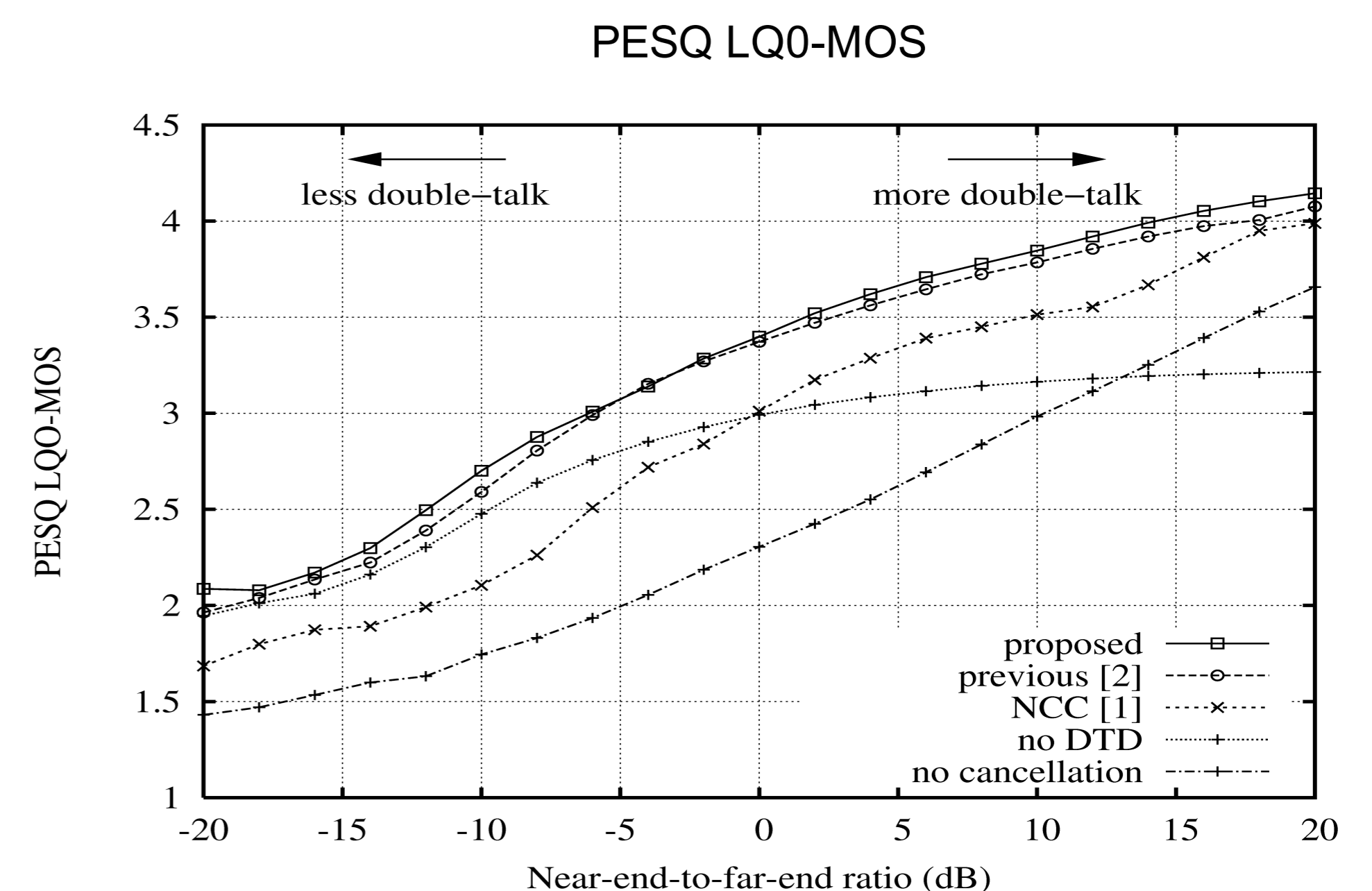
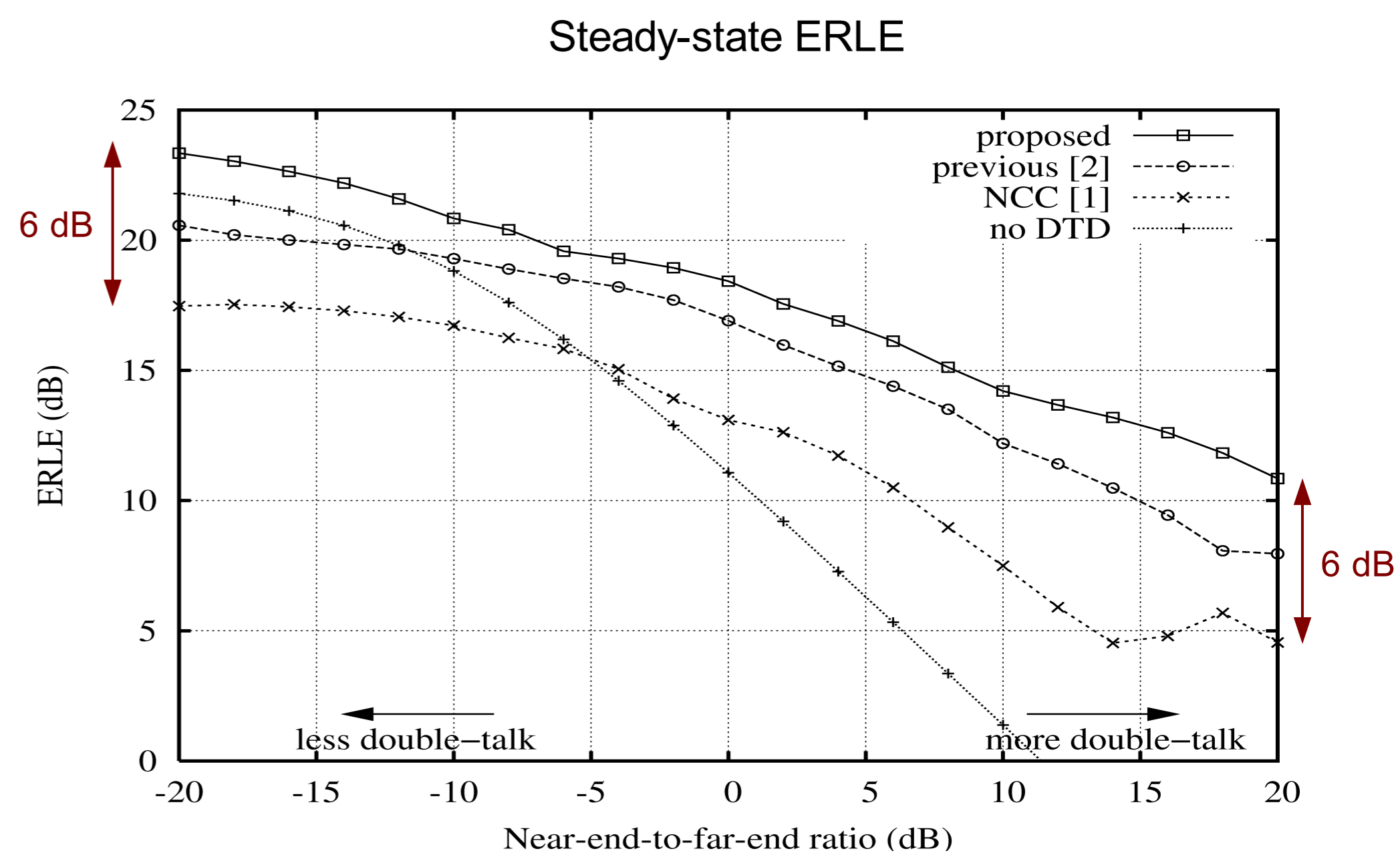
smoothed gradient

### Analysis

- $ERLE \approx 1/\eta$
- When gradient direction is stable,  $\eta$  increases
- When gradient alternates,  $\eta$  decreases
- Double-talk:  $e(n)$  increases abruptly,  $\eta$  constant
- Echo path change: gradient stabilises,  $\eta$  increases
- Reacts quickly to double-talk because  $\eta$  only tracks ERLE

### Results

- Tested on a 32-second speech sample
- Background noise and double-talk (-20 dB to +20 dB)
- Echo path change at 16 seconds
- Outperforms explicit double-talk detection by ~6 dB
- Able to adapt at all time
- Outperforms direct ERLE estimation by ~2 dB
- Less subject to estimation errors



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